Divide and Conquer Sorting Algorithms

1. Consider three implementations of Quicksort:
   a) A recursive version that picks an arbitrary element as the median.
   b) A recursive version that uses median of three partitioning.
   c) A non-recursive version that handles smaller sub-arrays first (using an explicit stack).

   For each of these alternatives, what is the average maximum stack depth when sorting a random array with 1000 elements?

2. Find the average number of sub-arrays of size 0, 1 and 2 when Quicksort is used to sort a random array with 1000 elements.

3. Quicksort and Mergesort can perform noticeably faster when insertion sort is used to handle small sub-arrays. Find a good cut-off M for the size of arrays that should be handled by insertion sort in your computer. Present timings or total number of comparisons that result for different settings of M to justify your answer.