

*Biostatistics 666*  
*Statistical Models in*  
*Human Genetics*

**Instructor**  
**Gonçalo Abecasis**

# *Course Logistics*

Grading

Office Hours

Class Notes

## Course Objective

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- Provide an understanding of statistical models used in gene mapping studies
- Survey commonly used algorithms and procedures in genetic analysis

# Assessment

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- 10-12 Weekly Assignments
  - About 60% of the final mark
- 2 Half Term Assessments
  - About 40% of the final mark

## Office Hours

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- Please cross out times for which you are unavailable in the sheet going around
- Room M4132  
School of Public Health II

## Class Website

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- PDF versions of notes and problem sets

[www.sph.umich.edu/csg/abecasis/class/](http://www.sph.umich.edu/csg/abecasis/class/)

- Please let me know about any mistakes!

# *Course Contents*

**Brief Overview**

## Genetic Mapping

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“Compares the inheritance pattern of a trait with the inheritance pattern of chromosomal regions”

### **Positional Cloning**

“Allows one to find where a gene is, without knowing what it is.”



## Some of the Topics Covered

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- Maximum Likelihood
- Modeling Genes in Populations
- Modeling Genes in Pedigrees

# Modeling Genes in Populations

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- Hardy Weinberg Equilibrium
- Linkage Disequilibrium
- The Coalescent
- Methods for Haplotyping

# Modeling Genes within Pedigrees

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- Elston-Stewart algorithm
- Lander-Green algorithm
- Genetic linkage tests
- Checking Genetic Data for Errors
- Family Based Association Tests

*Let's Get Started!*

**The Basics**

# Today – Primer In Genetics

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- How information is stored in DNA
- How DNA is inherited
- Types of DNA variation
- Common designs for Genetic studies

## DNA – Information Store

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- Encodes the information required for cells and organisms to function and produce new cells and organisms.
- DNA variation is responsible for many individual differences, some of which are medically important.

# Human Genome

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- Multiple chromosomes
  - 22 autosomes
    - Present in 2 copies per individual
    - One maternally and one paternally inherited copy
  - 1 pair of sex chromosomes
    - Females have two X chromosomes
    - Males have one X chromosome and one Y chromosome
- Total of  $\sim 3 \times 10^9$  bases (each A, C, T or G)

# Inheritance of DNA

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- Through recombination, a new “DNA string” is formed by combining two parental DNA strings
- Thus, each chromosome we carry is a mosaic of the two chromosomes carried by our parents
- Only a small number of changeovers between the two parental chromosomes
  - On average ~1 per Morgan ( $\sim 10^8$  bases)
- Copying of DNA sequences is imperfect and, for typical sequences, the error rate is about 1 per  $10^8$  bases copied



# Human Variation

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- Every chromosome is unique ...
- ... but when two chromosomes are compared most of their sequence is identical
- About 1 per 1,000 bases differs between pairs of chromosomes in the population
  - In the same individual
  - In the same geographic location
  - Across the world

# DNA Sequences That Vary...

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- Genes (protein coding sequences, which total <2% of all DNA)
  - ~30,000-35,000 in humans
- Pseudogenes
  - Ancient genes, inactivated through mutation
- Promoters and Enhancers
  - Sequences which control gene expression
- Repeat DNA
  - Useful for tracking DNA through families or populations
- Packaging sequences, “spacer” DNA, etc.

# Important Vocabulary ...

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- Locus
- Polymorphism
- Allele
- Mutation
- Linkage
- Genetic Marker
- Genotype
- Phenotype
  - Mendelian Traits
  - Complex Traits
- Chromosomal landmarks
  - Centromeres
  - Telomeres
- Gene
- RNA
- Protein

# Data for a Genetic Study

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- Pedigree
  - Set of individuals of known relationship
- Observed marker genotypes
  - SNPs, VNTRs, microsatellites
- Phenotype data for individuals

# Genetic Markers

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- Genetic variants that can be measured conveniently
- Typically, we characterize them by:
  - Number of Alleles
  - Frequency of Each Allele
  - These are summarized by the heterozygosity
- The most commonly used genetic markers are microsatellites and SNPs

# Phenotypes

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- Measured characters of individuals
- Mendelian Phenotypes
  - Completely determined by genes
  - e.g. Cystic Fibrosis, Retinoblastoma
- Complex Phenotypes
  - Controlled by multiple genes and environmental factors
  - eg. Diabetes, Inflammatory Bowel Disease

# Ultimate Aim of Gene-Mapping Experiments

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- Localize and identify variants that control interesting traits
  - Susceptibility to human disease
  - Phenotypic variation in the population
- The difficulty...
  - Testing several million variants is impractical...

## 3 Common Questions

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- Are there genes influencing this trait?
  - Epidemiological studies
- Where are those genes?
  - Linkage analysis
- What are those genes?
  - Association analysis



# Is a trait genetic?

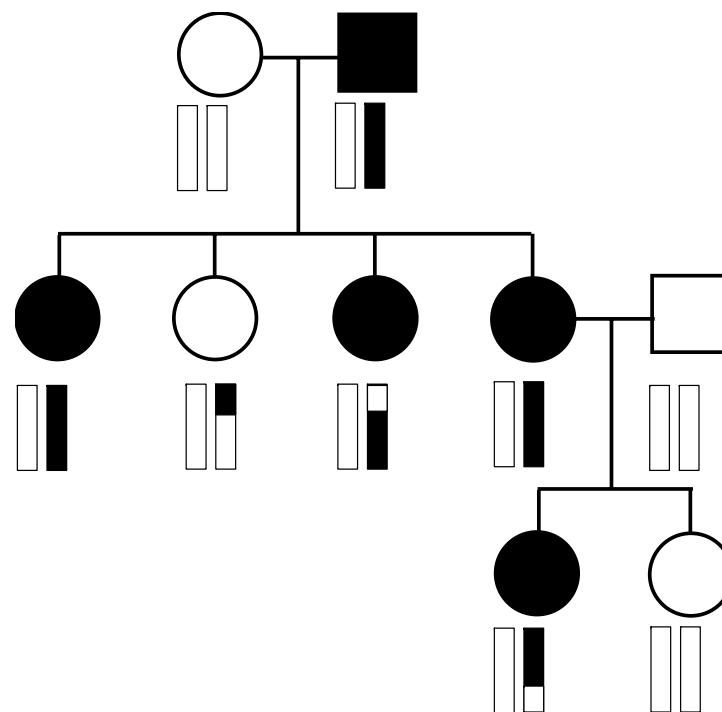
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- Examine distribution of trait in the population and among relatives
- E.g. Inflammatory Bowel Disease (Crohn's)
  - General population
    - 1-3 cases per 1,000 individuals
  - Twins of affected individuals
    - 44% of monozygotic twins also have Crohn's
    - 3.8% of dizygotic twins also have Crohn's

## Where are those genes?

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- Find genetic markers that co-segregate with disease
- E.g. D16S3136 co-segregates with Crohn's



## What are those genes?

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- Identify genetic variants that are associated with disease...
- E.g. Mutations which disrupt NOD2 are much more common in Crohn's patients

	Crohn's	Controls
● Arg702Trp:	11%	4%
● Gly908Arg:	4%	2%
● Leu1007fs	8%	4%

# Common Designs for Genetic Studies

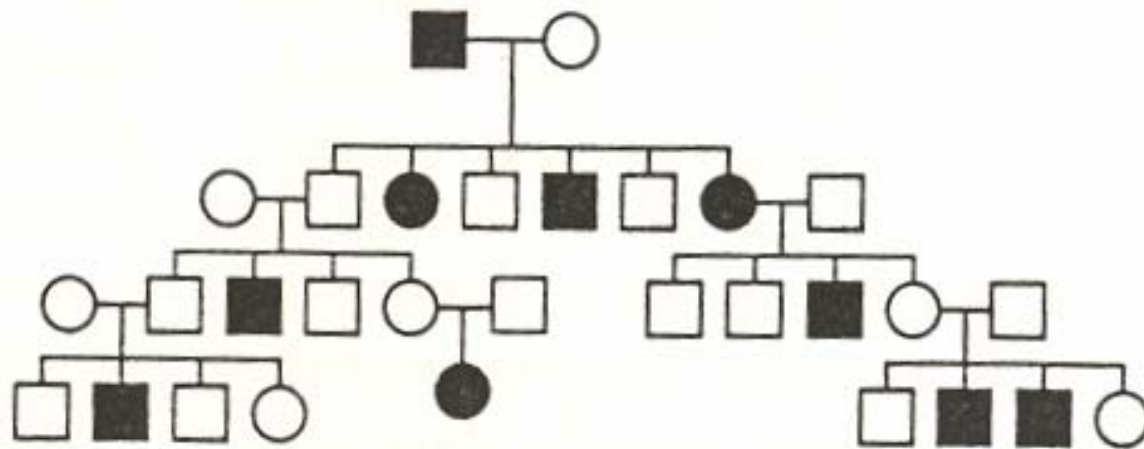
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- Parametric Linkage analysis
- Allele-sharing methods
- Association analysis

# Parametric Linkage Analysis

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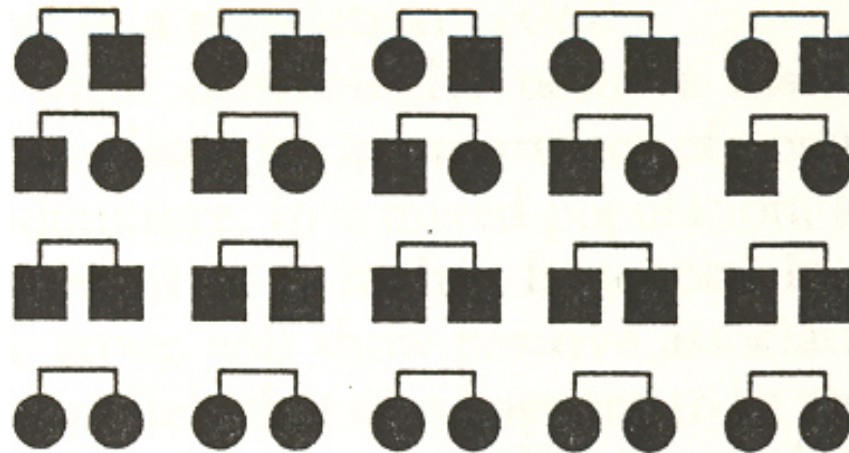
- Evaluate a specific model and location
  - Allele frequencies at disease loci
  - Probability of disease for each genotype
- Potentially very powerful
- Vulnerable to heterogeneity, model misspecification



# Allele Sharing Analysis

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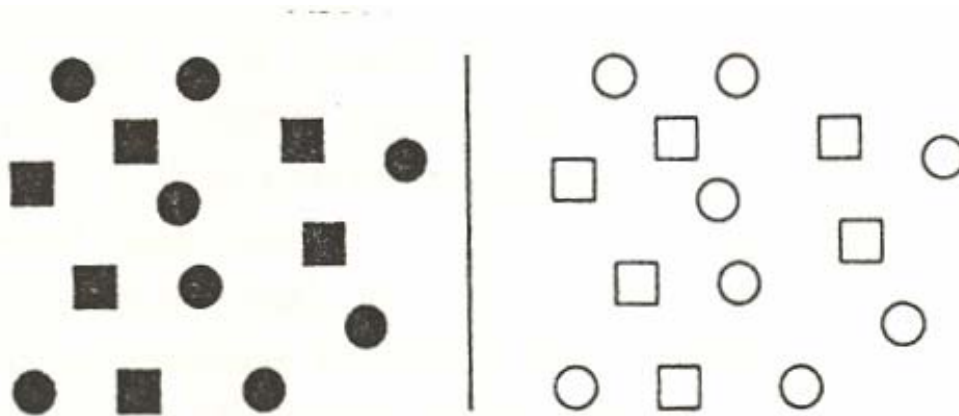
- Reject null hypothesis that sharing is random at a particular region
- Less powerful, but more robust
- Quantitative trait extensions exist



# Association Analysis

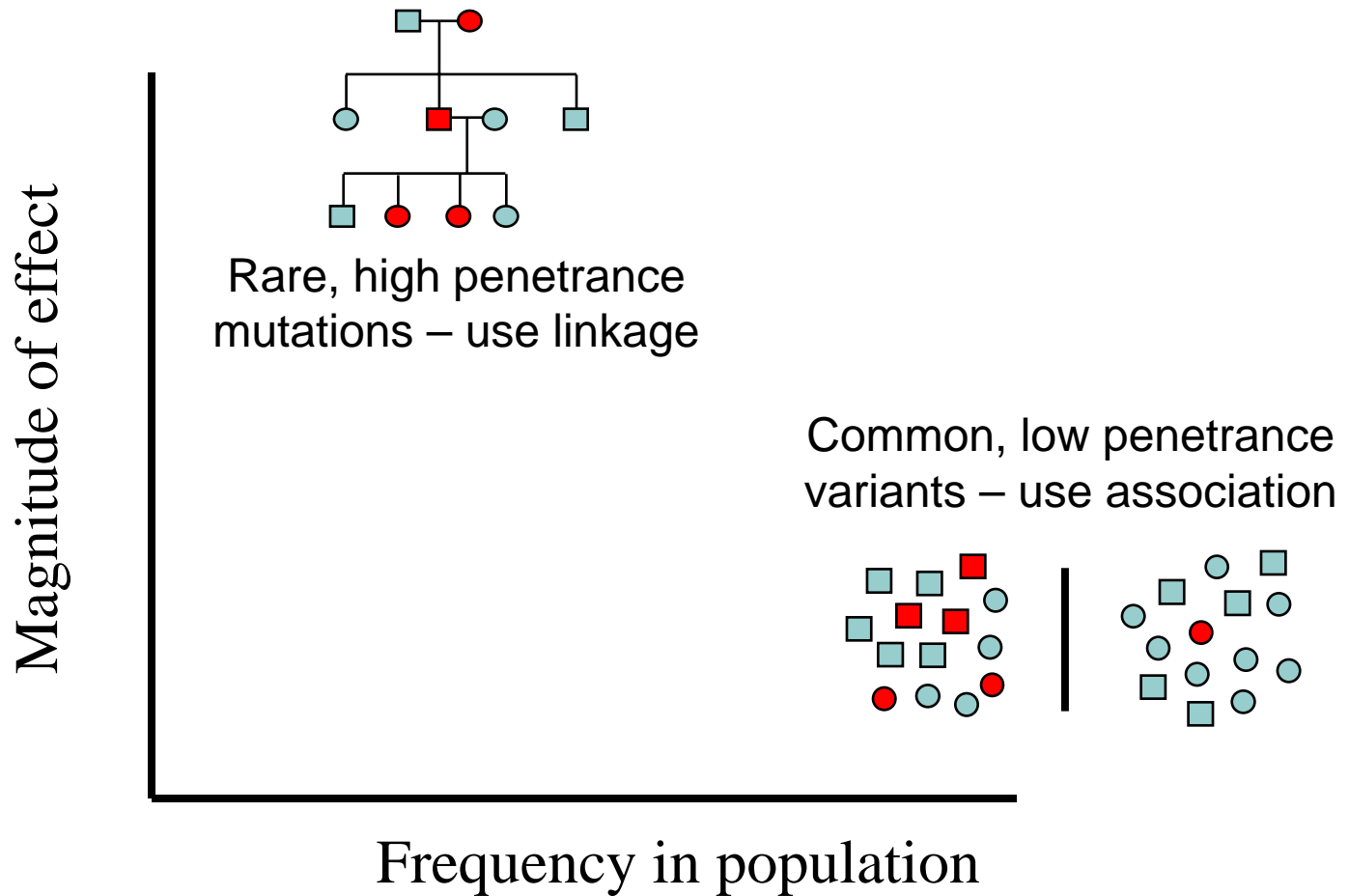
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- Simplest case compares frequency of allele among cases and controls
- Genome-wide search requires hundreds of thousands of markers
- Typically, focuses on candidate genes



# Which Design to Choose?

The Right Choice Depends on the Alleles We Seek...





# Genetic Linkage Studies

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- Identify variants with relatively large contributions to disease risk
- Require only a coarse measurement of genetic variation
  - 400 – 800 microsatellites can extract most of the linkage information in typical pedigrees
  - Until recently, the only option for conducting whole genome studies
- High-throughput SNP genotyping has already sped up and facilitated these studies
  - Data analysis methods must select subset of independent SNPs or model disequilibrium between markers

# Genetic Association Studies

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- Identify genetic variants with relatively small individual contributions to disease risk
- Require detailed measurement of genetic variation
  - > 10,000,000 catalogued genetic variants, so ...
  - Until recently, limited to candidate genes or regions
    - A hit-and-miss approach...
- SNP resources and decreasing assay costs now make it possible to examine 100,000s of markers

# Recommended Reading

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- An introduction to important issues in genetics:
  - Lander and Schork (1994)  
*Science* **265**:2037-48
- A good reference on molecular genetics:
  - Human Molecular Genetics  
Tom Strachan and Andrew Read

# Reading for Next Lecture

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- Will be discussing Hardy-Weinberg equilibrium
  - A basic feature of genotypes in human populations
- Wigginton, Cutler, Abecasis (2005)  
A note on exact tests of Hardy-Weinberg equilibrium.  
*Am J Hum Genet* **76**:887-93
- This paper describes an efficient method for testing Hardy-Weinberg equilibrium and includes many important historical references